

Optimal Load Shedding Using an Ensemble of Artificial Neural Networks

Original Scientific Paper

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Abstract – Optimal load shedding is a very critical issue in power systems. It plays a vital role, especially in third world countries. A sudden increase in load can affect the important parameters of the power system like voltage, frequency and phase angle. This paper presents a case study of Pakistan's power system, where the generated power, the load demand, frequency deviation and load shedding during a 24-hour period have been provided. An artificial neural network ensemble is aimed for optimal load shedding. The objective of this paper is to maintain power system frequency stability by shedding an accurate amount of load. Due to its fast convergence and improved generalization ability, the proposed algorithm helps to deal with load shedding in an efficient manner.

Keywords – ensemble of artificial neural network, load shedding, power system stability

1. INTRODUCTION

In this modern era, power consumption is increasing extensively with each passing day. A growing population with the need of more new plazas and buildings is responsible for greater energy consumption. An increase in power demand requires construction of more and more grids, and third world countries do not have enough resources to cope with this problem. The method to deal with this problem in order to gain system stability is to shed some load. This process is known as load shedding.

Optimal load shedding is defined as the curtailment of minimum load for each subsystem so that poise of demand and supply remain conserve [1]. When the load increases, generators connected to the power system slow down results in frequency decay. The threshold frequency value in Pakistan is 49.5 Hz. A decrease in frequency below the threshold value results in shutting down the generators. The shutting down of a generator in an interconnected system can trigger the failure of other parallel generators. This condition is known as a cascaded failure or blackout [2].

The case when system generation is greater than system demand causes the frequency to rise up [1]. An increase in frequency above the threshold value results in speeding up the generator until it burns out as shown in Figure 1.

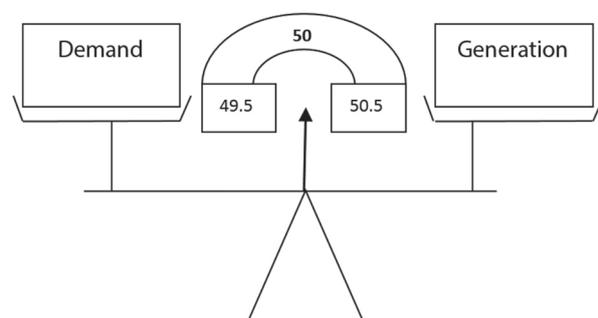


Fig. 1. Relation of frequency with generation and demand

When the load increases, the first action is performed by the governor that adjusts the speed by increasing the fuel quantity to recover the slow speed of the machine. In the case when the governor is not able to com-

compensate for declining frequency, load shedding is the final and ultimate solution [3]. There are several ways to shed load, like the breaker interlock method, under the frequency relay and programmable logic controller [4]. The disadvantages of these methods are that they are too slow and not highly efficient when disturbances and losses in the system are included during real-time calculation of load [5].

Many algorithms have been applied for optimal load shedding for maintaining the steady state of the power system. Results obtained by traditional methods take more time as compared to artificial neural networks (ANN) [6]. This method can determine the amount of load shedding magnitude in each step simultaneously that leads to a higher speed than traditional methods [5]. The error in the learning of an artificial neural network can be reduced by ensembling neural networks which will increase the accuracy of the system [7]. Optimal load shedding using an artificial neural network ensemble is the outcome of this research. In this paper, the Bootstrap Aggregating (Bagging) algorithm with Disjoint Partition is used to ensemble an ANN because of its fast convergence and low variance [8].

2. RELATED WORK

The basic idea of an ANN comes from the biological nervous system. ANNs are considered to be a simplified model of a biological neural network. ANNs are trained so that a specific input leads to a specific output target. It has to be trained to find a nonlinear relation between an input and an output. The basic layout of an ANN consists of an input layer, a hidden layer and an output layer.

The first step in designing the ANN is to find out the architecture that will yield best possible results. The size of the hidden layer is mostly 10% of the input layer [9]. Data transmission from the input layer to the output layer is shown in Figure 2.

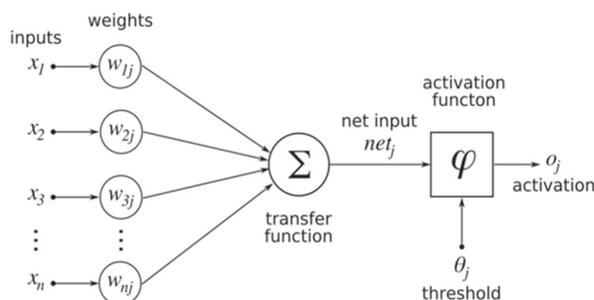


Fig. 2. Activation and flow of information in an ANN

Each of the ANN inputs has a specified weight which is indicated by w_0 , w_1 and w_2 , respectively. These weights are the strength of inputs and they determine the intensity of the input signal. The summation function decides how inputs and their weights are combined. Sometimes an activation function or bias is added in order to get the threshold value. The threshold

value is determined by the type of the transfer function. The summation function is compared with the threshold value; if the sum is greater than this threshold value, the output signal will be activated and vice versa. The desired output is compared with the ANN output and the difference between these two outputs is called error. The error is propagated backward to adjust the input weights in order to match the neural output with the desired one.

Nakawiro et al. [10] proposed the Ant Colony Optimization (ACO) technique for optimal load shedding. In this algorithm, the authors achieved load shedding by observing load variation at various buses by voltage stability margin; ACO will decide which load of which particular bus will be shed. A high speed makes this technique superior to other conventional methods. The shortcoming of this technique is its high complexity and convergence time is very high.

Chawla et al. [11] proposed a genetic algorithm (GA) for optimal load shedding. In this algorithm, load shedding is used to prevent voltage stability. A power world simulator is used to analyze the continuation of the power flow that helps determine load shedding. The GA will decide how much load will be shed at each bus. This algorithm is very easy to understand and it does not require much knowledge of mathematics. The shortcoming of this algorithm is the occurrence of data overfitting and it is too slow for real-time cases where long training is required.

3. ENSEMBLE OF ARTIFICIAL NEURAL NETWORK

An Ensemble of Artificial Neural Networks (EANN) consists of a number of ANN networks and an algorithm for combining their outputs [9]. Each individual network has a different input data set but the same target data set. After being combined and processed by the algorithm, the outputs of neural networks give the final EANN output.

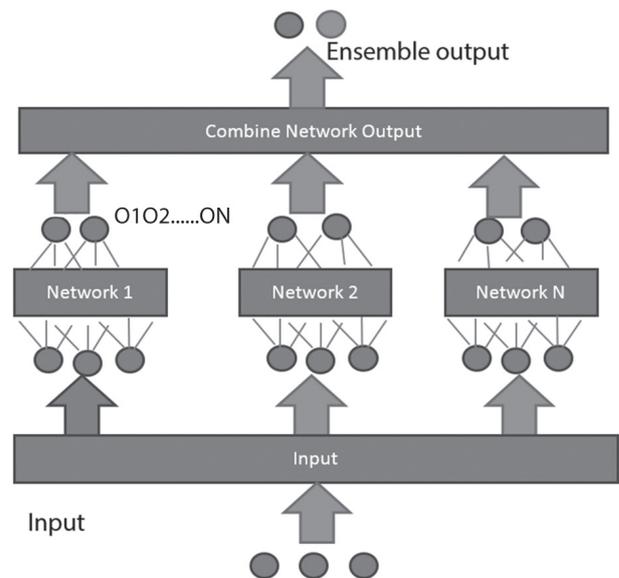


Fig. 3. Artificial neural network ensemble

There are many algorithms to ensemble ANNs [12]. In this research, Bootstrap Aggregating (Bagging) is used to ensemble ANNs. This algorithm depends on majority voting and different classifiers are combined by taking their means as shown in Figure 4:

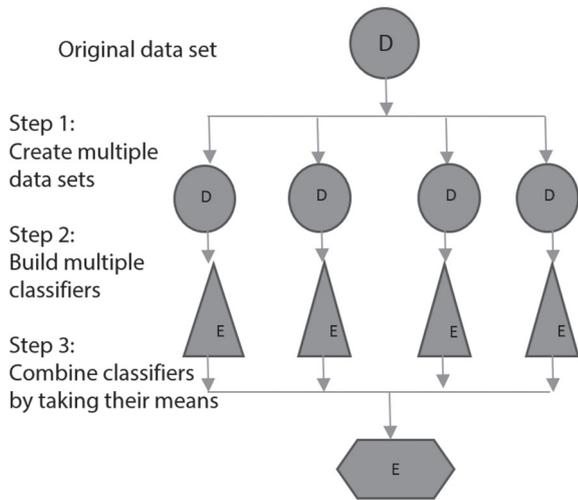


Fig. 4. General idea of bagging

Bagging is classified in two ways, i.e.; i) small bags, and ii) disjoint partition [13]. The small bags algorithm works such that subsets of the original data set may not be equal to the original data set. A disadvantage of small bags is the probability of repeating the number more than once. Disjoint partition makes the subsets of original data sets such that the number of the subset shall be equal to the original data set. Disjoint partition is considered to be more effective and accurate compared to small bags [13], [14]. The original data set is shown in Figure 5:

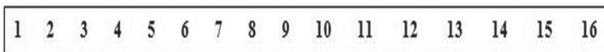


Fig. 5. Original data set

In a disjoint partition case, each particular number from the original data set is selected such that no repetition occurs, as shown in Figure 6:



Fig. 6. Disjoint partition

4. PROBLEM MOTIVATION

It is well-known that prediction can be improved by combining results of several predictors. In comparison to ANNs, EANNs always improve the results. EANN prediction will only be incorrect when the majority of ANN prediction data sets proves to be wrong. If the majority of prediction of ANNs proves to be wrong, then there is a problem in the data set [7, 15].

The output of an ANN does not match with the target function even after several trainings. The difference

between the actual and the target output is called error. The reason for this error lies in the learning process. Three main factors of errors in learning are bias, variance and noise [6].

$$\text{Error} = \text{Noise} + \text{Bias} + \text{Variance} \quad (1)$$

Large bias causes underfitting of data, while high variance causes overfitting of data [8]. Compared to a single classifier, grouping of classifiers may teach a more expressive concept class resulting in the reduction of bias [14], [15]. Results are relatively less dependent on a single training data set that results in variance reduction. Generalization of data to opt new data will increase when bias and variance are cut to a minimum and data will not suffer from over- and underfitting.

5. THE PROPOSED METHOD

The procedure to be adopted in this scenario has the following three steps:

1. Real data set generation,
2. Design of an ANN,
3. Design of an EANN.

Step 1: In this paper, a real-data set of one complete day of the Water and Power Development Authority (WAPDA), Pakistan, has been used. Data is provided by the National Power Control Centre (NPCC) Islamabad that monitors and controls each and every parameter of the power system. This data set includes power generation (PG), power demand (PL) and the rate of change of frequency (df/dt) shown in Table 1 and load management presented in Table 2.

Table 1. PG, PL and df/dt

Time	Total Generation	Total Demand	Frequency Decay
00:00:00 s	8151.2	11651.22	-0.22
01:00:00 s	7891.6	11394.93	-0.20
02:00:00 s	7725.8	11225.8	-0.50
03:00:00 s	7696.3	11196.3	-0.28
04:00:00 s	7713.12	11213.12	-0.29
05:00:00 s	8521.29	11694.62	0.16
06:00:00 s	9524.38	11524.39	-0.30
07:00:00 s	9897.81	11897.76	-0.09
08:00:00 s	9536.1	11746.1	-0.07
09:00:00 s	9792.77	12392.88	-0.15
10:00:00 s	9800.39	12400.39	-0.16
11:00:00 s	9828.43	12428.48	-0.02
12:00:00 s	9826.83	12426.85	-0.01
13:00:00 s	9555.35	12155.39	0.00
14:00:00 s	9796.15	12396.14	-0.04
15:00:00 s	9659.27	12259.21	0.03
16:00:00 s	9510.74	12110.77	-0.15
17:00:00 s	9568.38	12543.49	-0.03
18:00:00 s	9886.25	13386.21	0.07
19:00:00 s	9723.15	13223.17	-0.03
20:00:00 s	9726.16	12801.17	-0.15
21:00:00 s	9272.85	12272.83	-0.08
22:00:00 s	8809.23	11809.23	0.17
23:00:00 s	8424.41	11157.92	0.14

The rate of change of frequency can be calculated as [5]:

$$\frac{df}{dt} = \frac{\Delta P}{2H} \cdot f_0, \quad (2)$$

where

f_0 = permissible frequency,

$$\Delta P = \text{change in power } \Delta P = \frac{P_D - P_G}{P_G}, \quad (3)$$

P_D = power demand,

P_G = power generation,

H = inertial constant.

H is the machine inertia constant that varies from machine to machine [5]. Larger inertia causes less frequency to decay. It can be calculated from the equation (4):

$$H = \frac{H_1 * MVA_1 + H_2 * MVA_2 + \dots + H_n * MVA_n}{MVA_1 + MVA_2 + \dots + MVA_n} \quad (4)$$

The main reason for load shedding is not only short generation but distribution constraints and transmission constraints are also responsible. Transmission constraints are zero as NTDC transmits the entire load it receives; DISCO's constraints are not zero because of grid bottlenecks. Every power system has some spinning reserve, i.e., generators are not running at full speed. The WAPDA has no spinning reserve (Emergency L/M), as shown in Table (2).

In case of underfrequency load shedding, the total amount of load shed can be calculated from the equation (5):

$$LS = \frac{\frac{L}{1+L} - d \left(1 - \frac{f}{f_0}\right)}{1 - d \left(1 - \frac{f}{f_0}\right)}, \quad (5)$$

where

f = standard frequency in Pakistan,

f_0 = permissible frequency,

L = rate of overload per unit.

L can be calculated as:

$$L = \frac{\text{Total demand} - \text{Total Generation}}{\text{Total Generation}} \quad (6)$$

d = load reduction factor.

Load shed against each hour by the NPCC is shown in the table below and can also be calculated from the above equations. This load shed is taken as the output for ANN training.

Step 2: Before creating a neural network, selection of inputs and the target function is required. In this paper, PG, PL and df/dt are selected as inputs, while load shed during each hour is selected as the target. Specification of the ANN structure is presented in Table 3.

Table 2. Load management

LOAD MANAGEMENT						
Time (sec)	Short Generation (MW)	Transmission O/L (NTDC) (MW)	Industrial Cuts (MW)	DISCO'S Constraints (MW)	Emergency L/M (MW)	Total (MW)
0000	1167	0	24	1272	0	2463
0100	1095	0	14	1266	0	2375
0200	1160	0	14	1240	0	2414
0300	1068	0	17	1262	0	2347
0400	1024	0	18	1271	0	2313
0500	977	0	17	1261	0	2255
0600	1091	0	141	1255	0	2487
0700	1318	0	93	1230	0	2641
0800	1468	0	182	1201	0	2851
0900	1520	0	80	1172	0	2772
1000	1685	0	43	1086	0	2814
1100	1700	0	182	1168	0	3050
1200	1709	0	188	1166	0	3063
1300	1735	0	100	1209	0	3044
1400	1629	0	50	1191	0	2870
1500	1481	0	90	1231	0	2802
1600	1605	0	102	1282	0	2989
1700	1512	0	237	1182	0	2931
1800	1711	0	101	1207	0	3019
1900	1837	0	260	1097	0	3194
2000	1739	0	214	1093	0	3046
2100	1473	0	19	1105	0	2597
2200	1394	0	25	1139	0	2558
2300	1445	0	26	1231	0	2702

Table 3. ANN Specification

Number of input neurons	3 (PG, PL, df/dt)
Number of output neurons	1 (Pshed)
Number of hidden layer neurons	10
Neural network model	Feed forward back propagation
Training function	Levenberg-Marquardt back propagation (LMBP)
Adaptation learning function	Gradient descent with momentum weight and bias
Number of layers	2
Activation function for Layer 1	Trans-sigmoid
Activation function for Layer 2	Pure linear
Performance function	Mean square error (MSE)
Percentage of using information	Train (70%), test (15%), cross validation (15%)
Maximum of epoch	1000
Learning rate	0.01
Maximum validation failures	6
Error threshold	0.001
Weight update method	Batch

The LMBP training function is used in this research for training the ANN because it is considered as the fastest back propagation algorithm [16]. Gradient descent is used for adaptation learning that updates the mean weight and bias according to the batch method. Gradient descent is used to minimize the mean square error.

$$mse = \frac{1}{n} \sum_{i=1}^n e(i)^2 = \frac{1}{n} \sum_{i=1}^n (t_i - y_i)^2, \quad (7)$$

where

n = the number of examples,

t_i = the desired target value,

y_i = target output.

Gradient:

$$\nabla E[w] = \left[\frac{\sigma E}{\sigma w_0}, \frac{\sigma E}{\sigma w_1}, \dots, \frac{\sigma E}{\sigma w_n} \right] \quad (8)$$

The training rule:

$$\Delta w = -\eta \nabla E[w] \quad (9)$$

$$\Delta w_i = -\eta \frac{\sigma E}{\sigma w_i} \quad (10)$$

Update:

$$w_i = w_i + \Delta w_i, \quad (11)$$

where

E is an error,

w is the weight of input vectors, and

η is a learning rate.

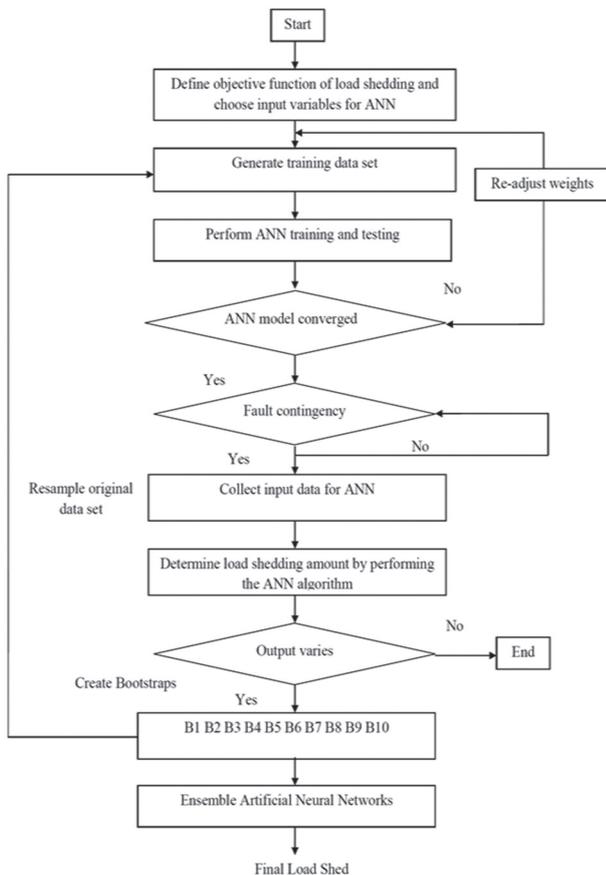


Fig. 7. Flowchart of optimal load shedding using the EANN

The training data set is used to adjust ANN weights, 75% of data is used for training purposes, while 15% is used for validation to avoid overfitting of data. The testing set is used for testing the final solution in order to predict the actual output of the neural network.

Step 3: MATLAB is used to create bootstraps from the original data set to ensemble the ANN. In this paper, ten bootstraps are created by disjoint partition. Ten different bootstraps are trained that, having ten different neural network outputs, are then combined by taking their means. The final predicted EANN output gives the value of load shed. When this final predicted value is compared with the previously trained neural network values, the percentage error is reduced to a minimum.

6. RESULT SIMULATION

This section includes plots of the first neural network, the first bootstrap. The first bootstrap that simply resamples the original data set is shown in Table 4.

Table 4. The first bootstrap

First Bootstrap		
Power Generation (MW)	Power Demand (MW)	Frequency Decay (seconds)
8809.23	12534.49	-0.2
9828.43	12426.85	-0.15
9510.74	11694.62	-0.28
8521.29	12400.39	0.14
9536.10	11809.23	-0.15
8151.20	12259.21	-0.16
7696.30	11746.10	-0.22
9568.38	13223.17	-0.50
7713.12	13386.21	0.00
9792.77	11651.22	-0.03
9800.39	12396.14	-0.09
7891.60	11157.92	-0.02
9659.27	11897.76	-0.08
9555.35	12392.88	0.07
9272.85	11213.12	-0.29
9723.15	11225.80	-0.30
9897.81	12801.17	-0.01
9886.25	12272.83	-0.03
9796.15	11196.30	0.16
9826.83	11394.93	-0.07
8424.41	12110.77	-0.15
7725.80	12428.39	0.03
9524.38	11524.39	-0.04
9726.16	12155.39	0.17

The divider and the function used for dividing data are shown in Figure 8. The LMBP training method is used with the mean square error (MSE) performance function.

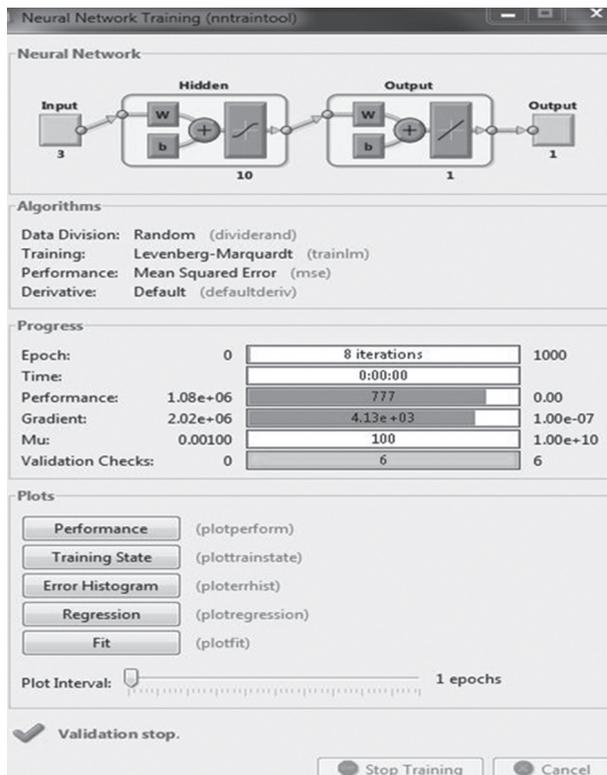


Fig. 8. ANN training window

The regression plot presents the relation between the desired output (Target) and the actual output (ANN output). For an ideal case, the data should be within the 45 degree line, where ANN outputs are equal to targets.

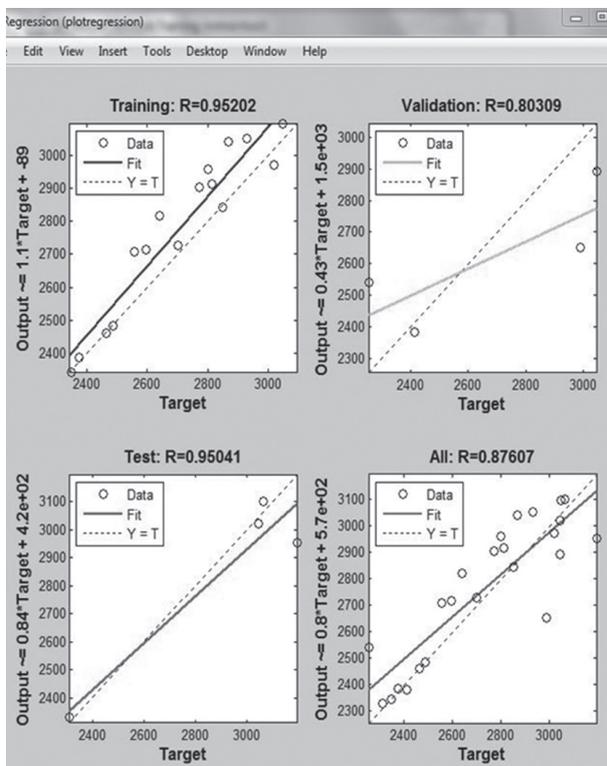


Fig. 9. ANN regression plot

The first neural network output and the percentage errors are shown in Table 5:

Table 5. ANN output and % error

NN1 Output	% Errors
2588.146349	0.0484
2711.167012	0.1240
2313.741919	0.0433
2497.484983	0.0603
2463.103022	0.0609
2905.432884	0.2239
3662.615851	0.3210
3108.166746	0.1503
2762.270979	0.0321
2800.228241	0.0101
2838.334945	0.0086
2555.398179	0.1936
2560.946318	0.1960
2660.746810	0.1440
2561.016882	0.1206
2647.375219	0.0584
2746.761337	0.0882
2643.432732	0.1088
2756.426501	0.0953
2502.151551	0.2765
2450.702934	0.2429
2654.883259	0.0218
2879.407539	0.1116
2838.853948	0.0482

After creating ten different neural networks and by creating their bootstraps, all neural networks are combined by the bagging algorithm. The predicted EANN output is closer to the target value when compared to the predicted ANN value. This comparison implies that the percentage error of an ensemble output is smaller.

Table 6. EANN output and % error

Ensemble Output (EO)	Ensemble % Error
2491.504434	0.007458354
2646.946619	0.002739744
2523.905181	0.043545685
2403.053650	0.098366643
2394.548802	0.010851551
2425.999743	0.022932324
2694.164820	0.076893892
2715.635443	0.027483602
2754.423904	0.035062176
2788.343257	0.005861279
2786.175262	0.009986715
2786.346057	0.004623545
2784.539434	0.000102378
2800.665490	0.086884532
2791.466720	0.028133339
2784.988816	0.006108170
2889.617498	0.071473061
2852.844219	0.027395741
2880.139671	0.085916665
2859.472524	0.011989226
2832.979901	0.075192944
2622.204930	0.020131302
2604.972773	0.019440973
2790.174601	0.077870650

The EANN results are more accurate not only for the first neural network but also for all remaining seven neural networks.

The second and the third ANN output are compared with the EANN output in Table 7:

Table 7. Comparison of the 2nd and the 3rd ANN output with the EANN output

NN2 Output	% Errors	NN3 Output	% Errors	EO	% Error
2492.122209	0.0117	2918.041571	0.1559	2661.50	0.0074
2370.790193	0.0180	2585.629010	0.0815	2646.94	0.0027
1760.727638	0.3710	2422.175714	0.0340	2523.90	0.0435
2102.709566	0.1162	2407.539358	0.2510	2603.05	0.0983
2070.927034	0.1169	2419.376117	0.0440	2594.54	0.0108
3151.053893	0.2844	3166.272959	0.2878	2925.99	0.0229
3157.66764	0.2124	2294.824446	0.0837	2694.16	0.0768
2868.252121	0.0792	2406.313788	0.0975	2715.63	0.0274
3187.317963	0.1055	2499.540409	0.1406	2754.42	0.0350
3060.356414	0.0942	2616.476639	0.0594	2788.34	0.0058
3050.397740	0.0775	2612.738227	0.0770	2786.17	0.0099
3042.827062	0.0024	2639.117652	0.1557	2786.34	0.0046
3038.898886	0.0079	2638.082587	0.1611	2784.53	0.0001
3144.737487	0.0320	2606.716779	0.1678	2800.66	0.0868
3066.224015	0.0640	2635.924572	0.0888	2791.46	0.0281
3090.515658	0.0934	2612.841860	0.0724	2784.98	0.0061
3202.412036	0.0666	2530.012925	0.1814	2789.61	0.0714
3100.376931	0.0546	2686.600772	0.0910	2852.84	0.0273
2949.389031	0.0236	2663.787944	0.1333	2780.13	0.0859
3015.461480	0.0592	2680.396677	0.1916	2859.47	0.0119
3074.356027	0.0920	2682.307639	0.1356	2832.97	0.0751
3187.364507	0.1852	2695.658172	0.0366	2873.20	0.0201
3014.81893	0.1515	2863.563957	0.1067	2904.97	0.0194
3545.632153	0.2379	3097.950495	0.1278	2930.17	0.077

Figure 10 shows a comparison of the percentage error of the NN2 output and the EANN output. It is very much clear from Figure 10 that the ensemble output is closer to the target value.

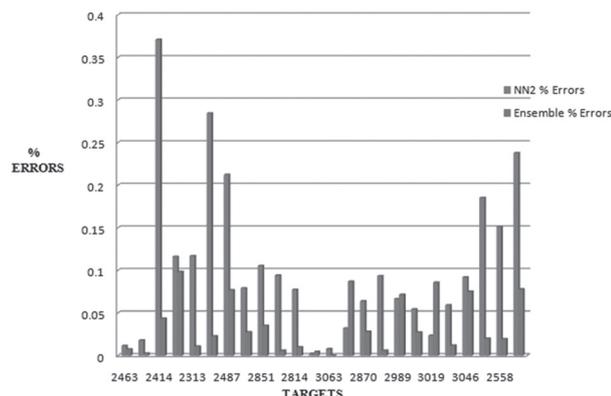


Fig.10. % Errors of NN2 and the EANN

Figure 11 shows the regression plot of the EANN in which the value of R represents the relation between the output and the target. R=1 suggests the exact relation between the output and the target, while R=0 implies that there is no relation at all between the two.

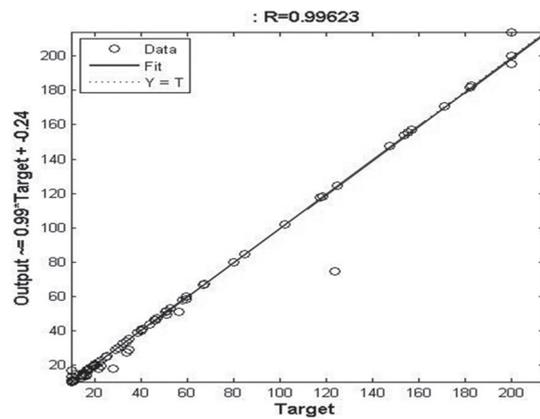


Fig. 11. Regression plot of the EANN

7. CONCLUSION

In this paper, optimal load shedding has been proposed based on the EANN algorithm. The occurrence of fault and an increase in demand are two prominent cases of load shedding in the power system. Extensive literature referring to ANN based load shedding has shown that the techniques presented so far do not deal with optimal load shedding so efficiently. In the proposed technique, an effort has been made to fill this technological gap.

It is shown that when the EANN is used to deal with load shedding, a great deal of improvement is witnessed compared with the ANN. The EANN shows an increase in the performance gain in terms of convergence. By looking at the results, it has been found out that the bagging algorithm for the EANN reduces variance to a minimum. ANNs perform accurately for the given training data but, when the training data set changes for the next hour, the ANN faces some problems like over- or underfitting. These issues may disturb system accuracy during load shedding or may disrupt power system stability. To overcome these problems, to increase system accuracy and generalization ability of the ANN, the EANN technique has been used.

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